



编程语言的设计原理

Design Principles of Programming Languages

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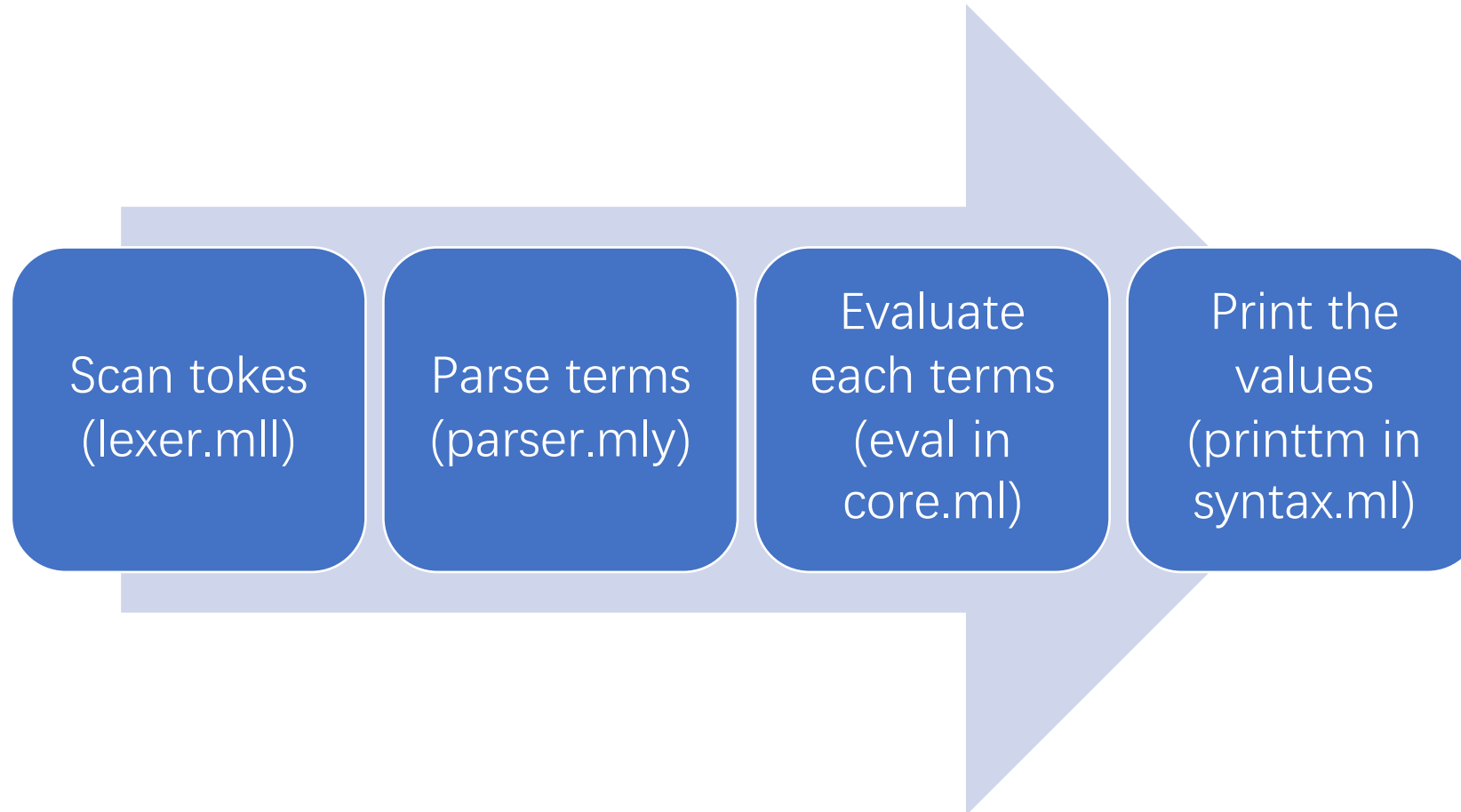
Practice in Class

arith, fullsimple, fullref



Structure of package

main.ml drives the whole process





Structure of package

syntax. ml defines the terms

```
type term =  
  TmTrue of info  
| TmFalse of info  
| TmIf of info * term * term * term  
| TmZero of info  
| TmSucc of info * term  
| TmPred of info * term  
| TmIsZero of info * term
```

Info:

a data type recording *the position* of the term in the source file



Structure of package

let rec isnumericval t = match t with

 TmZero(_) → true

 | TmSucc(_,t1) → isnumericval t1

 | _ → false



Structure of package

- eval in core.ml

```
let rec eval t =  
  try let t' = eval1 t  
    in eval t'  
  with NoRuleApplies → t
```

- **eval1**: perform a single step reduction



Some abbreviations

- UCID = upper case identifier
- LCID = lower case identifier
- ty = type
- tm = term
- LCURLY = “{“
- RCURLY = “}”
- USCORE = “_”



Commands

- Each line of the source file is parsed *as a command*
 - type command = | Eval of info * term
 - New commands will be added later

- Main routine for each file

```
let process_file f =  
  alreadyImported := f :: !alreadyImported;  
  let cmds = parseFile f in  
  let g c =  
    open_hvbox 0;  
    let results = process_command c in  
  print_flush();  
  results  
in  
  List.iter g cmds
```




Homework for 3/9

- Please get familiar with OCaml and its utilities
- Please download the implementation package of the TAPL, and digest the source codes in archives of *arith*, *tyarith*, *untype*.
- Please give your implementation for Chap. 4
 - Submit your code as a compressed file with one of the above names
 - Your submission should contain file `test.f` that contains exactly the expressions to be tested
 - TA will perform the following two commands to verify your submission:
 - `make`
 - `./f test.f`



Exercise arith.simple_use

- Using arith to write the following equation
 - Return five if two is not zero, otherwise return nine
 - Hint: read the code in *parser.mly*



Exercise arith.size

- Make the *evaluation* computes *the size of a term* (3.3.2) instead of reducing the term, and test it on the original test.f
 - Hint:
 - `pr: string->unit` prints a string to the screen
 - `string_of_int : int->string` converts an integer into a string
 - Remember to change both .ml and .mli files



Big-step vs small-step

- Big-step is usually easier to understand
 - called “natural semantics” in some articles
- Big-step often leads to *simpler proof*
- Big-step **cannot describe computations** that *do not produce a value*
 - Non-terminating computation
 - “Stuck” computation



Exercise arith.big-step

- Change the evaluation to use *big-step semantics*, and compute the following expressions:
 - true;
 - if false then true else false;
 - if 0 then 1 else 2;
 - if true then (succ false) else 2;
 - 0;
 - succ (pred 0);
 - iszero (pred (succ (succ 0)));



fullsimple

- Implementing all extensions in Chapter 11
- Allow different types of command:
 - Evaluation: type-checking and reducing a term
 - Bindings
 - Variable binding: `a: Int;`
 - Type variable binding: `T;`
 - Term abbreviation binding: `t = succ 0;`
 - Type abbreviation binding: `T = Nat -> Nat;`
- Types can be used without declaration (uninterpreted types)

`x: X`

`(lambda a: X. a) x`



Review: nameless representation

- What is the nameless representation of the following term?

$$\lambda x. x (\lambda y. x y)$$
$$\lambda. 0 (\lambda. 1 0)$$



Fullsimple, terms

type term =

TmVar of info * int * int

| TmAbs of info * string * ty * term

| TmApp of info * term * term

| ...

- Using *nameless representation of terms*
- The *second int* for TmVar is used for debugging
 - = the number of items in the context
- The “*string*” in TmAbs is used for printing



Example: printing terms

and printtm_ATerm outer ctx t = match t with

| TmVar(fi, x, n) ->

if ctxlength ctx = n then

pr (index2name fi ctx x)

else

pr ("[bad index: " ^ ...

| TmAbs(fi, x, tyT1, t2) ->

(let (ctx',x') = (pickfreshname ctx x) in

obox(); pr "lambda ";

pr x'; pr ":"; printty_Type false ctx tyT1; pr "."; ...

printtm_Term outer ctx' t2; ...



Review: context

- What contexts are used in our course?
 - Mapping names to integers in nameless representation
 - Σ : mapping variables to types
- Can be combined into one
- New contexts in the implementation
 - Type variable binding: marking type variables
 - Term abbreviation binding: Mapping variables to terms (and their types)
 - Type abbreviation binding: Mapping type variables to terms

```
type binding =  
  NameBind  
  | TyVarBind  
  | VarBind of ty  
  | TmAbbBind of term * (ty option) |  
  TyAbbBind of ty  
  
type context = (string * binding) list
```

Auxiliary functions for nameless representation



- `name2index`
 `info->context ->string->int`
 return the index of a name
- `index2name`
 `info->context ->int->string`
 inverse of the above
- `pickfreshname`
 `context->string ->(context, string)`
 generate a fresh name using the second parameter as hint

```
type binding =  
  NameBind  
  | TyVarBind  
  | VarBind of ty  
  | TmAbbBind of term * (ty option) |  
  TyAbbBind of ty  
  
type context = (string * binding) list
```



Exercise fullsimple.nameless

- Construct a term t that is evaluated a term t' in fullsimple, where t' is different from t via only alpha-renaming (i.e., no beta-reduction)



Exercise fullsimple.match

- Add pattern matching for *tuples*, and test on the following expressions
 - `let {x, y, z} = {true, 1, {2}} in z;`
 - `let {x, y, z} = {true, 1, {2}} in (lambda x:Nat. x) y;`
 - `let {x, y, z} = let x = 1 in {true, x, {2}} in z;`
 - `lambda x:Nat. let {x, y} = {true, 1} in x;`
 - `let x = 0 in let {y, z} = {1, 2} in x;`
 - `let {y, z} = {1, 2} in let y = 3 in y;`
- Part of the code is already provided to you in the following two pages



Partial code for fullsimple.match

- Adding the following line to “type term =” in syntax.ml
 - | TmPLet of info * string list * term * term
- Adding the following lines after line 235 in parser.mly
 - | LET Pattern EQ Term IN Term
{ fun ctx -> TmPLet(\$1, \$2, \$4 ctx, \$6 (List.fold_left (fun x y -> addname x y) ctx \$2)) }
 - Pattern :
LCURLY MetaVars RCURLY
{ \$2 }
| LCURLY RCURLY
{ [] }
- Add the following line to tminfo in syntax.ml
 - | TmPLet(fi,_,_,_) -> fi



Partial code for fullsimple.match

- Adding the following lines to “printtm_Term” in syntax.ml

```
| TmPLet(fi, xs, t1, t2) ->
obox0();
pr "let {";
let rec print xs =
match xs with
  x::x'::rest -> pr x; pr ","; print (x'::rest);
  | x::[] -> pr x;
  | [] -> pr ""; in
print xs;
pr "} = ";
printtm_Term false ctx t1;
print_space(); pr "in"; print_space();
let ctx' = List.fold_left (fun ctx x -> addname ctx x) ctx xs in
printtm_Term false ctx' t2;
cbox()
```